

# South American Journal of Logic



**Scope of the Journal**

The aim of the South American Journal of Logic is to promote logic in all its aspects: philosophical, mathematical, computational and historical, by publishing high quality peer-reviewed papers.

This journal will encourage interaction among logicians based in South America and also between logicians from South America and logicians from other continents.

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